

# 1. Math Functions

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## Syntax Guide to MATH FUNCTIONS

### Calculus

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$\partial$	$\partial\langle\text{name}\rangle(\langle\text{expr}\rangle)$ <i>x, expression</i>	----->	<i>derivative of the expression with respect to variable x</i>
$\int$	$\int(\langle\text{R}\#\rangle, \langle\text{R}\#\rangle, \langle\text{expr}\rangle, \langle\text{name}\rangle)$ <i>a, b, expression, x</i>	----->	<i>integral from a to b of expression with respect to x</i>
TAYLOR	TAYLOR( $\langle\text{expr}\rangle, \langle\text{name}\rangle, \langle\text{N}\#\rangle$ ) <i>expression, x, n</i>	----->	<i>Taylor polynomial about x = 0 of order n</i>

### Complex

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ARG	ARG( $\langle\text{C}\#\rangle$ ) <i>complex number</i>	----->	<i>argument of complex number [i.e., if the complex number z has polar form (r, t), then ARG(z= t)]</i>
CONJ	CONJ( $\langle\text{C}\#\rangle$ ) <i>complex number</i>	----->	<i>conjugate of complex number</i>
IM	IM( $\langle\text{C}\#\rangle$ ) <i>complex number</i>	----->	<i>imaginary part</i>
RE	RE( $\langle\text{C}\#\rangle$ ) <i>complex number</i>	----->	<i>real part</i>

### Constant

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(These take no arguments; they are special numbers with special names.)

e	the base of the natural log (rounded to 2.71828182846)
i	(0,1) the standard square root of -1
MAXREAL	the constant 9.9999999E499 <i>(largest positive real number that can be represented on the HP38G)</i>
MINREAL	the constant 1.0000000E499 <i>(smallest positive real number that can be represented on the HP38G)</i>
$\pi$	the constant n (rounded to 3.14159265359)

## Hyperb

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ACOSH	ACOSH(<#>)		
	$X$	----->	<i>inverse hyperbolic cosine of x</i>
ASINH	ASINH(<#>)		
	$X$	----->	<i>inverse hyperbolic sine of x</i>
ATANH	ATANH(<#>)		
	$X$	--- ----->	<i>inverse hyperbolic tangent of x</i>
COSH	COSH(<#>)		
	$X$	----->	<i>hyperbolic cosine of x</i>
SINH	SINH(< # >)		
	$X$	----->	<i>hyperbolic sine of x</i>
TANH	TANH(<#>)		
	$X$	----->	<i>hyperbolic tangent of x</i>
ALOG	ALOG(<#>)		
	$X$	----->	$10^x$

NOTE: More accurate than the usual operation

EXP	EXP(<#>)		
	$X$	----->	$e^x$

NOTE: More accurate than the usual operation  $e^x$

EXPM1	EXPM1 (< # >) "exponential of # minus one"		
	$X$	----->	$exp(x) - 1$

NOTE: More accurate near  $x=0$  than with usual operations.

LNP1	LNP1(< # >) logarithm of (# plus one)"		
	$X$	----->	$ln(x + 1)$

NOTE: More accurate near  $x = 0$  than with usual operations.

## List

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CONCAT	<p>CONCAT(&lt; {} &gt; , &lt; {} &gt;) Concatenate two lists.</p> $\{x_1, \dots, x_n\}, \quad \text{-----} > \quad (x_1, \dots, x_n, y_1, \dots, y_m)$ $\{y_1, \dots, y_m\}$ <p>NOTE: Joins two lists end to end to make a new list.</p>
$\Delta$ LIST	<p><math>\Delta</math>LIST(&lt; {} &gt;) List of "first differences"</p> $\{x_1, x_2, \dots, x_n\} \quad \text{-----} > \quad \{x_2 - x_1, x_3 - x_2, \dots, x_n - x_{(n-1)}\}$
$\Pi$ LIST	<p><math>\Pi</math>LIST (&lt; {} &gt;) Product of elements</p> $\{x_1, \dots, x_n\} \quad \text{-----} > \quad x_1 * x_2 * \dots * x_n$
$\Sigma$ LIST	<p><math>\Sigma</math>LIST (&lt; {} &gt;) Sum of elements</p> $\{x_1, \dots, x_n\} \quad \text{-----} > \quad x_1 + x_2 \dots + x_n$
MAKELIST	<p>MAKELIST(&lt; expr &gt; , &lt; name &gt; , &lt; # &gt; , &lt; # &gt; , &lt; # &gt; )  <i>expression, variable name, starting value, end value, step size</i>            ----- &gt;  <i>(expr   (name = start), expr   (name = start + step), ..., expr   (name = end))</i></p> <p>NOTE: Creates a list by evaluating the expression for each value of the variable name obtained by stepping from the starting value to the end value by the step size.</p> <p style="text-align: right;">EXAMPLE:</p> <p>MAKELIST(X^2,X,1,5,2) creates {1,9,25}</p>
POS	<p>POS(&lt; {} &gt; , &lt; N# &gt;) Position of value in list</p> $\{x_1, \dots, x_n\}, y \quad \text{-----} > \quad \textit{index value } i \textit{ such that } x_i = y,$ <p style="text-align: right;">or 0 if no such I exists</p>
SIZE	<p>SIZE(&lt; {} &gt; )</p> $\textit{list} \quad \text{-----} > \quad \textit{size of the list (\# of elements)}$
SORT	<p>SORT(&lt; {} &gt; )</p> $\textit{list} \quad \text{-----} > \quad \textit{list sorted in increasing order}$

## Loop

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ITERATE	ITERATE(< expr >, < name >, < R# >, < N# >) <i>expression, name, x0, n ----- &gt;</i> iterates the function expression in variable name n times starting with input x0 EXAMPLE: ITERATE(X^2,X,5,3) results in 390625 because we have $5^2 = 25$ , $25^2 = 625$ , and $625^2 = 390625$ .
RECURSE	RECURSE(< name>, <expr>, <N#>, <N#>) <i>index variable, Nth term, first term, second term</i> ----- > allows you to store a sequence definition from within a program or from the HOME screen. EXAMPLE: RECURSE(N, N^2, 1, 4) STO> U1(N)
$\Sigma$	$\Sigma$ (< name > = < N# >, < N# >, < expr >) <i>index n, starting index n1, ending index n2, expression for nth term</i> ----- > summation of expression in index variable n from $n = n1$ to $n = n2$

## Matrix

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COLNORM	COLNORM(<M#>) <i>matrix [[M]]</i> ----- > column-norm of M
COND	COND(<M#>) <i>matrix [M]</i> ----- > condition number of M
CROSS	CROSS(<V#>, <V#>) <i>vectors [v1], [v2]</i> ----- > cross-product of v1 and v2
DET	DET (<M#>) <i>matrix [M]</i> ----- > determinant of M
DOT	DOT (<V#>, <V#>) <i>vectors [v1], [v2]</i> ----- > dot-product of v1 and v2
EIGENVAL	EIGENVAL(<M#>) <i>matrix [[M]]</i> ----- > [eigenvalues] (vector of eigenvalues of M)

<b>Matrix</b>	<b>Continued</b>
EIGENVV	EIGENVV(<M#> matrix <i>[[M]]</i> -----> <i>{[[eigen vectors]], [eigen values]}</i> NOTE: list of matrix of eigenvectors and a vector of eigenvalues
IDENMAT	IDENMAT (<N#> Integer <i>n</i> -----> <i>Creates an nxn identity matrix</i>
INVERSE	INVERSE (<M#> Matrix <i>[[M]]</i> -----> <i>multiplicative inverse M<sup>-1</sup></i>
LQ	LQ(< M# > matrix <i>[[M]]</i> -----> <i>{ [[L]] [[Q]] [[P]] }</i>
LSQ	LSQ(<M#>, <M#> matrices <i>[[B]], [[A]]</i> -----> <i>matrix [[X]]</i> Note: X is the least squares solution of A* X= B
LU	LU(<M#> matrix <i>[[M]]</i> ----- > <i>{ [[L]] [[U]] [[P]] }</i> NOTE: result is list of three matrices L, U, and P, where P*L*=M and L is lower-triangular, U is upper-triangular with 1's on the main diagonal, and P is a permutation matrix
MAKEMAT	MAKEMAT(<expr>, <n1#>, <n2#> expression in I and J, n1 (number of rows), n2 (number of columns) -----> <i>matrix M(I,J) where the (I,J) entry is the value of the expression</i>
QR	QR<M#> matrix <i>[[M]]</i> -----> <i>{ [[Q]] [[R]] [[P]] }</i> NOTE: result is list of three matrices G, R, and P, where Q is orthogonal, R is triangular, and P is a permutation
RANK	RANK(<M#> matrix <i>[[M]]</i> ----- > <i>computed rank of M</i>
ROWNORM	ROWNORM(<M#> matrix <i>[[M]]</i> ----- > <i>row-norm of M</i>
RREF	RREF(<M#> matrix <i>[M]</i> -----> <i>reduced row-echelon form of M</i>

<b>Matrix</b>	<b>Continued</b>
SCHUR	SCHUR(<M#> <i>matrix</i> <b>[[M]]</b> ----->        { <b>[[Q]]</b> <b>[[U]]</b> } NOTE: result is list of two matrices where $Q^*U^*Q^H = M$
SIZE	SIZE(<M#> <i>matrix</i> <b>[[M]]</b> -- ----->        (n1, n2) (size of the matrix M)
SPECNORM	SPECNORM(<M#> <i>matrix</i> <b>[[M]]</b> ----->        spectral norm of M
SPECRAD	SPECRAD(<M#> <i>matrix</i> <b>[M]</b> ----->        spectral radius of M
SVD	SVD(< M# > <i>matrix</i> <b>[[M]]</b> ----->        { <b>[[U]]</b> <b>[[V]]</b> <b>[S]</b> } NOTE: result is a list of two matrices and a vector where $U^H * M * V^H = \text{diag}(S)$ and $U * \text{diag}(S) * V = M$
SVL	SVL(<M#> <i>matrix</i> <b>[[M]]</b> ----->        vector <b>[S]</b> NOTE: Result is the vector [S] described in SVD as above
TRACE	TRACE(<M#> <i>matrix</i> <b>[[M]]</b> ----->        trace of M
TRN	TRN(<M#> <i>matrix</i> <b>[M]</b> -----> <i>matrix transpose of M</i>

## Polynom

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POLYCOEF	POLYCOEFF(<V#> [Rn, ..., R1] vector of roots	----->	[An, ... A1, A0] vector of coefficients
	NOTE:		The r's are the roots of the polynomials $aNx^N + A(N-1) * x^{N-1} + \dots = a1x + a0$
POLYEVAL	POLYEVAL(<V#>, <#>) [aN, ..., a1, a0], r vector of coefficients, real number	----->	$aNr^N + \dots + A1R + A0$ value of polynomial
POLYFORM	POLYFORM(<expr>, <name.>, <name> ..., ) expression, x, y, ... ,	----->	expression
	NOTE:		Result is a polynomial in x whose coefficients are Polynomials in y whose coefficients are ...
	EXAMPLE:		POLYFORM(X^2 * Y^2 + X^2 * Y, X)
			Results in the polynomial (Y^2 + Y) * X^2
POLYROOT	POLYROOT(<V#>) [aN, ..., a0] vector of coefficients	----->	[rN, ..., r1] vector of roots
	NOTE:		The r's are the roots of the polynomial $aNx^N + A(N-1) * x^{N-1} + \dots + a1x + a0$

## Prob

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COMB	COMB(<N#>, <N#>) integers n, k	----->	combinations n choose k $\frac{(n * (n-1) * \dots * (n-k + 1))}{(1 * 2 * \dots * (k-1) * k)}$
!	(<N#>!) integer n	----->	factorial n! (1 * 2 * ... * n)
PERM	PERM(<N#>, <N#>) Integers n, k	----->	permutations $n * (n - 1) * \dots * (n - k + 1)$
RAND	RAND No arguments	----->	random # between 0 and 1

<b>Prob</b>	<i>Continued</i>	
UTPC	UTPC(< N#>, < R#>) integer N, real X	----- > upper-tail chi-square distrib. of order N evaluated at X
UTPF	UTPF(< N#>, < N#>, < R#>) integers N1, N2,	----- > upper-tail F-distrib. of real X order N1, N2, evaluated at X
UTPN	UTPN(< R#>, < R#>, < R#>) reals m, v, X	----- > upper-tail normal distrib. of mean m, variance v evaluated at X
UTPT	UTPT(< N#>, < R#>) Integer N, real X	----- > upper-tail student's T-distrib. N of order N evaluated at X

## **Real**

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CEILING	CEILING(< R#>) real number x	----- > least integer <sup>3</sup> x
DEG→RAD	DEG→RAD(< R#>) real number x	----- > convert x degrees to corresponding radians
FLOOR	FLOOR(< R# >) real number x	----- > greatest integer <sup>2</sup> to x
FNROOT	FNROOT(< expr >, < name >, < R# >) expression, x,x0	----- > r such that exp / (x = r) = 0. Search is started near x0.
FRAC	FRAC(< R#>) real number x	----- > fractional part of x
HMS→	HMS→(< expr >) real number x	----- > converts hours/minutes/ seconds format to decimal hours
→HMS	→HMS (< expr >) real number x	----- > convert decimal hours to hours/minutes/seconds format.

**Real***Continued*


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INT	INT(<R#> real number <i>x</i>	----- >	integer part of <i>x</i>
	EXAMPLE:		INT(23.438) returns 23 as result
MANT	MANT(<R#> real number <i>x</i>	----- >	mantissa of <i>x</i>
MAX	MAX(<R#>, <R#> real numbers <i>x</i> , <i>y</i>	----- >	maximum of <i>x</i> , <i>y</i>
MIN	MIN(<R#>, <R#> real numbers <i>x</i> , <i>y</i>	----- >	minimum of <i>x</i> , <i>y</i>
MOD	MOD(<N#> MOD <N#> integers <i>m</i> , <i>n</i>	----- >	integer remainder when <i>m</i> is divided by <i>n</i>
	EXAMPLE:		27 MOD 4 returns a result of 3
%	%(<R#>, <R#> real numbers <i>x</i> , <i>p</i>	----- >	$x * p * 0.01$
%CHANGE	%CHANGE(<R#>, <R#> real numbers <i>x</i> , <i>y</i>	----- >	$100 * (y-x) / x$
%TOTAL	%TOTAL(<R#>, <R#> real numbers <i>x</i> , <i>y</i>	----- >	$100 * y / x$
RAD→DEG	RAD→DEG (<R#> real number <i>x</i>	----- >	converts radians to degrees
ROUND	ROUND (<R#>, <N#> real <i>x</i> , integer <i>n</i>	----- >	rounds <i>x</i> to <i>n</i> units
SIGN	SIGN (<#> real or complex <i>x</i>	----- >	$x / ABS(x)$ if $x \neq 0$ 0 if $x = 0$
TRUNCATE	TRUNCATE (<R#>, <N#> real <i>x</i> , integer <i>n</i>	----- >	truncates <i>x</i> to <i>n</i> units
XPON	XPON (<R#> Real number <i>x</i>	----- >	exponent of <i>x</i> when written In scientific notation.

## Stat-Two

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PREDX	PREDX(< name >, < # >) <i>name, y</i> ----- > <i>predicted value for the "independent" variable of the indicated statistical dataset, given the "dependent" value</i>
PREDY	PREDY(< name >, < # >) <i>name, x</i> ----- > <i>predicted value for the "dependent" variable of the indicated statistical dataset, given the "independent" value</i>

## Symbolic

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=	This is an equational operator used to define equations like $A + C = C/2$ , but it is not a predicate (like $=$ in Test ).
ISOLATE	ISOLATE(< expr >, < name >) <i>expression or equation, name of a specific variable</i> ----- > <i>symbolic expression for specific variable in terms of the others</i> NOTE: An expression is interpreted as an equation with the expression on one side and 0 on the other side of the $=$ .
LINEAR?	LINEAR?(<name>) <i>expression name</i> ----- > <i>flag indicating whether the expression is linear</i>
QUAD	QUAD(< expr >, < name >) <i>quadratic expression or equation, name of a specific variable</i> ----- > <i>symbolic expression for the two complex roots</i> NOTE: An expression is interpreted as an equation with the expression on one side and 0 on the other side of the $=$ .
QUOTE	QUOTE(<expr>) <i>expression</i> ----- > <i>Suppress the expression eval.</i> NOTE: Single quote marks also work as in '<expr>'
(WHERE)	<expr>  (<name> = < # >, <name> = < # >, ...) "substitution" <i>expression x, p 1, y, p2,...</i> ----- > <i>expression evaluated where x =p 1, y =p2, etc.</i>

## Test

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<	<R#> < <R#> a, b	----- >	1 if $a < b$ , 0 otherwise
≤	<R#> ≤ <R#> a, b	----- >	1 if $a \leq b$ , 0 otherwise
==	<R#> == <R#> a, b	----- >	1 if $a = b$ , 0 otherwise
≠	<R#> ≠ <R#> a, b	----- >	1 if $a \neq b$ , 0 otherwise
>	<R#> > <R#> a, b	----- >	1 if $a > b$ , 0 otherwise
≥	<R#> ≥ <R#> a, b	----- >	1 if $a \geq b$ , 0 otherwise
AND	<R#> AND <R#> a, b	----- >	1 if both a and b ≠ 0, 0 otherwise
IFTE	IFTE(< predicate >, <true-clause >, < false-clause >) a, expression 1, expression 2	----- >	expression 1 if $a \neq 0$ expression 2 otherwise
NOT	NOT <R#> a	----- >	1 if $a = 0$ , 0 otherwise
OR	<R#>OR<R#> a, b	----- >	1 if a or b a non-zero 0 otherwise
NOR	<R#>XOR<R#> “exclusive or” a, b	----- >	1 if a a ≠ 0 or b ≠ 0, but not both, 0 otherwise

## Trig

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ACOT	ACOT(<#>)		
	x	----- >	<i>inverse cotangent of x</i>
ACSC	ACSC(<#>)		
	x	----- >	<i>inverse cosecant of x</i>
ASEC	ASEC(< # >)		
	x	----- >	<i>inverse secant of x</i>
COT	COT(< # >)		
	x	----- ~ >	<i>cotangent of x</i>
CSC	CSC(< # >)		
	x	----- >	<i>cosecant of x</i>
SEC	SEC(< # >)		
	x	----- >	<i>secant of x</i>

### **Functions which are not in the MATH menu and not on the keyboard:**

NEG            NEG(< # or V# or M# or {} or expr or grob >)  
NOTE: same functionality as -x key.